



**COLORADO SCHOOL OF MINES**  
**ELECTRICAL ENGINEERING DEPARTMENT**

**EENG577 Advanced Electric Machine Dynamics for Smart-Grid Systems**

**M3 Project: Synchronous Generator-abc**

A 659 MVA, 4-Pole, 20 kV, 0.9 P.F., Double-Y Connected (with grounded neutral), 60 Hz turbogenerator, whose armature and field winding parameters (neglecting saturation) are summarized as follows:

$r_s$	=	$7.4 \times 10^{-4} \Omega$	$r_f$	=	$0.0860 \Omega$
$r_{kd1}$	=	$1.58 \times 10^{-4} \Omega$	$L_{sv}$	=	$0.05 \times 10^{-3} \text{ H}$
$r_{kq1}$	=	$1.227 \times 10^{-4} \Omega$	$L_{mv}$	=	$0.05 \times 10^{-3} \text{ H}$
$L_{sa}$	=	$1.95 \times 10^{-3} \text{ H}$	$L_{ff}$	=	$444 \times 10^{-3} \text{ H}$
$L_{ma}$	=	$0.80 \times 10^{-3} \text{ H}$	$L_{akdm1}$	=	$0.447 \times 10^{-3} \text{ H}$
$L_{afm}$	=	$26.1 \times 10^{-3} \text{ H}$	$L_{akqm1}$	=	$0.670 \times 10^{-3} \text{ H}$
$L_{fkd1}$	=	$5.05 \times 10^{-3} \text{ H}$	$L_{kd1kd1}$	=	$0.1254 \times 10^{-3} \text{ H}$
$L_{kd1f}$	=	$6.29 \times 10^{-3} \text{ H}$	$L_{kq1kq1}$	=	$0.3762 \times 10^{-3} \text{ H}$

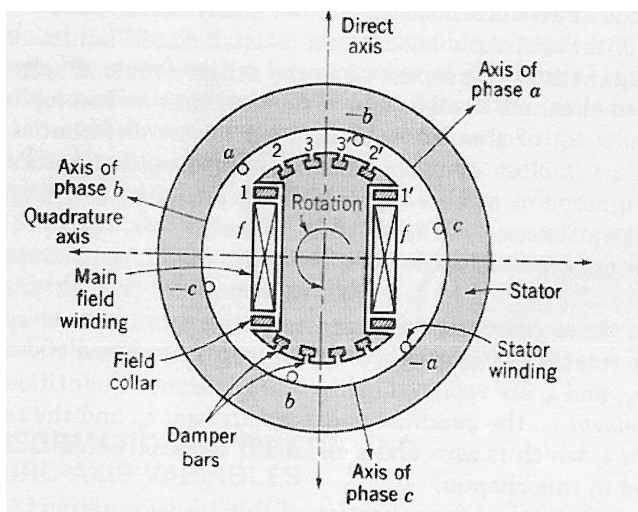
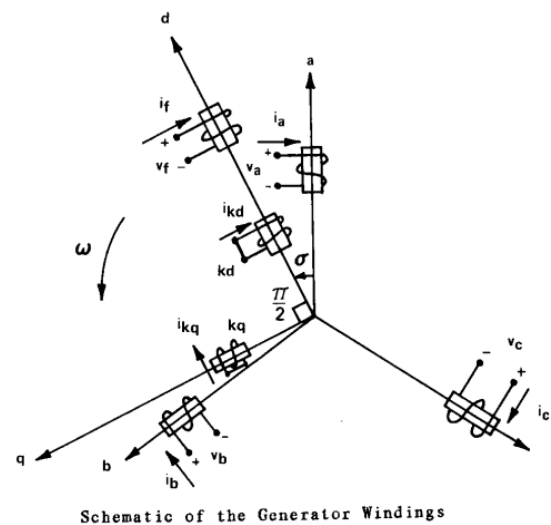


Fig-1: A Typical Machine Cross-section



Schematic of the Generator Windings

Fig-2 Schematic of Generator Windings

**PART I**

1. Show a cross-section of the synchronous machine and draw corresponding winding **schematic diagram** and label all axes (a, b, c, f, d, and q) properly.
2. Write down the State Space (SS) model in expanded matrix form, use the symbols in the lecture notes (**no values**) for the following:
  - i. Case-1: Neglect the effects of the damping circuits in your SS model. Include only windings a, b, c, and f.
  - ii. Case-2: Account for the effects of the damping circuits in your SS model. Include all windings a, b, c, f, kd1, and kq1.
3. Write the state space model in the form  $\dot{\underline{X}} = \underline{A} \bullet \underline{X} + \underline{B} \bullet \underline{U}$  using **compact matrix** notation, given in the course handouts. However, write the **expanded form** using expressions and **numerical values for matrices A and B** for:
  - i. Case-1: Neglect the effects of the damping circuits in your SS model. Include only windings a, b, c, and f.
  - ii. Case-2: Account for the effects of the damping circuits in your SS model. Include all windings a, b, c, f, kd1, and kq1.

**PART II**

Assuming that the machine is operating at its rated voltage, current, and power factor (overexcited) as a generator, calculate the necessary excitation field current **assuming**  $V_f = r_f i_f = 338 \text{ V}$ . Also, assume the angle  $\sigma$ , between phase a-axis and the d-axis is equal to zero (meaning in Figs 1 & 2, the a-axis is aligned with the d-axis). In addition, consider the terminal voltage (to neutral) of phase a,  $V_a$ , to be the reference in the phasor diagram (meaning having a phase angle equal to zero).

At time  $t=0.0$  the machine is connected to an infinite busbar where, a, b, and c phase voltages are given by:

$$v_a = \frac{20 \times 10^3}{\sqrt{3}} \sqrt{2} \cos(\omega t) \text{ Volts}$$

$$v_b = \frac{20 \times 10^3}{\sqrt{3}} \sqrt{2} \cos(\omega t - 2\pi/3) \text{ Volts}$$

$$v_c = \frac{20 \times 10^3}{\sqrt{3}} \sqrt{2} \cos(\omega t - 4\pi/3) \text{ Volts}$$

Assuming that the terminal voltage of the field winding is kept constant by the excitation control system at  $V_f = r_f i_f = 338 \text{ V}$ , and that the speed of the turbogenerator is maintained, by its prime mover, constant at its rated synchronous value:

1. Calculate the initial conditions (values at  $t=0 \text{ s}$ ) for  $i_a, i_b, i_c, i_f, i_{kd1}, i_{kq1}$

2. Perform analysis for the following cases:

- i. Neglect the effects of the damping circuits in your model. Calculate by means of numerical integration (MATLAB or Simulink) and *plot the profiles versus time over the first 30 cycles* for the following variables:  $i_a$ ,  $i_b$ ,  $i_c$ ,  $i_f$ , and  $T_{em}$ .
- ii. Include the effects of the damping circuits in your model. Calculate by means of numerical integration (MATLAB or Simulink) and *plot the profiles versus time over the first 30 cycles* for the following variables:  $i_a$ ,  $i_b$ ,  $i_c$ ,  $i_f$ ,  $i_{kd1}$ ,  $i_{kq1}$ , and  $T_{em}$

- **Discuss your results especially those of Part II**
- **Include MATLAB code or Simulink block diagram in an appendix**

Please Note: This is a group project, please make one group submission. You can discuss the problem with other class groups; however, each group should work independently.